

NAME:

1. If f is a differentiable function, find an expression for the derivative of $y = x^7 f(x)$.

Select the correct answer.

a. $\frac{d}{dx}(x^7 f(x)) = 7x^6 f(x) + x^7 f'(x)$

b. $\frac{d}{dx}(x^7 f(x)) = 7x^7 f(x) + x^6 f'(x)$

c. $\frac{d}{dx}(x^7 f(x)) = 7x^6 f(x) - x^7 f'(x)$

d. $\frac{d}{dx}(x^7 f(x)) = 7x^7 f(x) - x^6 f'(x)$

e. $\frac{d}{dx}(x^7 f(x)) = 6x^6 f(x) - x^7 f'(x)$

2. Find the given derivative by finding the first few derivatives and observing the pattern that occurs.

$$\frac{d^{99}}{dx^{99}}(\sin x) = \boxed{-\cos x}$$

3. Differentiate the function.

$$f(t) = (t + t^{-1})^3 = \left[3(t^2 + 1) \left(\frac{t^2 - 1}{t^4} \right) \right]$$

$$\frac{d}{dx} \left[t^3 + 3t^2 t^{-1} + 3t t^{-2} + t^{-3} \right]$$

power rule product rule product rule power rule